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Mindy Thomas and Guy Raz host NPR's first podcast for kids, "Wow in the World."

## Mathematical Mosaics

OPT ART: From Mathematical Optimization to Visual Design. Robert Bosch. 188 pp. Princeton University Press, 2019. \$29.95.

Held at arm's length, the illustration at the top of the facing page is easily recognized as a portrait of the 44th president of the United States. Closer examination reveals that the image is formed from blocks of white dots set against a black background. The dots are the white pips on dominos-specifically, "double nine" dominos, which have from zero to nine dots on each half of a rectangular tile (see detail below the portrait). A full set of double-nine dominos contains 55 pieces. The portrait of Barack Obama combines 44 such full sets, for a total of 2,420 tiles, arranged to create light and dark patterns that the eye interprets as an image.

Dominos first became a medium for this type of visual expression 40 years ago in the hands of Ken Knowlton, a computer scientist and artist at Bell Laboratories, whose work appeals to those who like a dash of math and algorithms with their artwork. Robert Bosch, the creator of the Obama portrait, takes this nerdish genre to a higher level of refinement. Starting from a black-and-white photograph or other monochrome image, his goal is not just to produce a good likeness but to find the best possible arrangement of the dominos-the configuration that most closely matches the pattern of shadow and light in the original, according to a mathematical measure. His recent book, Opt Art: From Mathematical Optimization to Visual Design, celebrates this idea of optimal or optimized graphic works,
along with the computational tools needed to create them.

To build the Obama mosaic, Bosch began with a photograph, using a 55 $\times 88$ grid to divide it into a total of 4,840 square regions. The range of gray levels in the image was compressed to 10 discrete values, labeled from 0 (the darkest) through 9 (the brightest). Then came the tricky part: placing the dominos on pairs of adjacent squares so that the number of pips in each square matched the assigned gray value as closely as possible. As the detail below the mosaic shows, there were many choices to be made, not only in selecting the best tile for each place but also in deciding how it should be oriented. At the end of the process every square needed to be covered, with no gaps or overlaps, and every domino in the 44 sets had to have a home somewhere in the picture.

How can you find the best possible arrangement of 2,420 double-nine dominos? Trying all possible configurations is not a feasible approach. Even working with just a single set of dominos, and ignoring some messy details of geometry and orientation, there are more than $10^{73}$ ways of placing the 55 tiles. To break through this combinatorial bottleneck, Bosch turned to methods known as linear optimization, or linear programming. "Linear" signifies that the solution space is bounded by straight lines or flat planes; no curves are allowed.

The problem-solving tools of linear optimization come out of a milieu far from the world of the arts. Historically, they are closely associated with business and economics, logistics, management, and military planning. An airline might use linear programming to match up aircraft, flight segments, and crew members. A chemical plant might use it to adjust its operations to yield the most profitable mix of products. Yet art, too, is an exercise in problem-solving


Forty-four sets of dominos have been arranged to create a portrait of the 44th president of the United States in an artwork by Robert Bosch. Levels of brightness and shadow in the portrait are represented by the number of pips on the dominos, ranging from zero to nine on each half of each tile. The pattern shown is the best possible according to a specific measure: For each square cell, square the difference between the number of pips and the desired level of brightness, then take the sum of all these values. The detail at right shows that the choices to be made include not only which tile goes where but also how the tiles are oriented. The version shown is a computergenerated image, but at least two groups of schoolchildren have reproduced this entire tableau using real dominos. From Opt Art.
and constraint satisfaction. Furthermore, constraints in the arts can be inspirations rather than obstacles. Bosch cites the example of Georges Seurat's pointillist painting A Sunday Afternoon on the Island of La Grande Jatte. "Seurat set himself the task of producing the best possible depiction of what he saw on the riverbank, subject to two highly restrictive, self-imposed constraints: he had to keep his colors separate, and he could only apply paint to the canvas with tiny, precise, dot-like brush strokes." It sounds a little like painting with dominos.


Bosch is a professor of mathematics at Oberlin College, where he teaches optimization (among other subjects). In Opt Art he gives a brief explanation of the underlying mathematics, based on a cute question: What can you build with a fixed supply of Lego bricks? He then introduces optimization procedures for some comparatively simple mosaics, in which each tile covers a single square, before turning to the more challenging domino tilings.

The narrative later turns to a quite different kind of data-optimizing art-
work: connect-the-dots drawings in which a scene is rendered by a continuous closed path that can be drawn without lifting the pen from the paper. The first step is to create the set of dots to be connected-typically several thousand of them-using a stippling technique in which a higher local density of dots will produce a darker region in the finished drawing. Drawing the path from dot to dot to dot and eventually back to the starting point is where optimization enters the problem. The objective is to find the shortest possible route for such a tour. This is one of the famous hard problems of computer science, known as the traveling salesman problem, which is not believed to have an efficient solution; nevertheless, linear optimization algorithms can find a good tour for problems of the size considered in Opt Art. With further work and ingenuity, it is often possible to prove that a tour is not only good but optimal. The illustration on page 186 shows four point sets on top and four corresponding optimal tours beneath them for a detail from Michelangelo's Creation of Adam.

I note in passing that the stippled versions of these drawings are actually more appealing to my eye than those with the traced paths. The al-


A connect-the-dots algorithm yields optimized line drawings (bottom four panels) for this detail from one of the panels of Michelangelo's Sistine Chapel ceiling painting, Creation of Adam. The starting point for each drawing is a stippled version (top four panels) of the original image, a version in which the local density of dots encodes the darkness of that region. The optimization step finds the shortest closed path that passes through all the dots. Each of four subtly different stipple patterns yields a noticeably different shortest path. From Opt Art.
gorithms for finding a good stipple pattern are also interesting. But in the stippling process there is no criterion for defining optimality; the choice of pattern is made by a more conventional kind of aesthetic judgment, based on what pleases the eye.

Bosch goes on to present a gallery of other graphic fantasies generated by various optimizing procedures, applying them to knots, knight's tours on the chessboard, labyrinths, and tilings that òbey additional constraints. One of my favorites is the idea of a "still-life tiling," based on John Horton Conway's Game of Life. The basic elements of the tableau are tiny black or white squares, called cells, arranged in a large grid. What sets the system apart from other tilings is that the cells interact with one another, changing their own color in response to the configuration of the surrounding cells. Bosch sets up patterns that are stable for a while and then slowly disintegrate as a result of these interactions, like a sand painting swept away by the wind.

Opt Art serves as an inviting introduction to a curious corner where art
and mathematics intersect. Bosch projects equal enthusiasm for both. The artwork is not just an ornament meant to attract a broader readership, and the math is not just a tool for producing pictures. For Bosch it's clear they both hold deep intrinsic interest, and he communicates this to the reader.

My one major disappointment with the book is that readers who want to experiment with these ideas for themselves may find too little guidance in it to make a successful start. Although Bosch supplies the key mathematical background, the practical details of turning basic principles into working computer programs are rather intimidating. Compounding this problem, Bosch does most of his work with the proprietary software package Gurobi Optimizer, which is available free to those with an academic affiliation but is probably beyond the means of other casual users. Suggesting a few alternatives would have been helpful.

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# Using Data to Understand the World 

THE ART OF STATISTICS: How to Learn from Data. David Spiegelhalter. 426 pp. Basic Books, 2019. \$32.

Can statistics be understood without mathematical formulas? Yes, up to a point. The Art of Statistics: How to Learn from Data, by David Spiegelhalter, is an introduction to the study of data and statistics for interested readers; it resembles in some ways an introductory textbook but is much less formal. The book emphasizes basic concepts and tools of data representation and leaves out the algebra.

Spiegelhalter has chosen to begin his book not with lessons on probability theory but with exemplary instances of reasoning with data. In an initial example, he discusses the case of an English physician, Harold Shipman, who in 1999 was convicted of murdering 15 of his patients. After the trial, Spiegelhalter and other statisticians were asked to conduct an inquiry into what additional crimes Shipman might have committed. They eventually determined that he had actually murdered at least 215 (mostly elderly) patients over a period of 24 years. Spiegelhalter shows that an exploration of the data regarding the patients who died reveals patterns that lead to insights into Shipman's behavior (see scatterplot on facing page). In a subsequent example, Spiegelhalter examines ship records from the Titanic to identify the combination of passenger characteristics associated with the highest rates of survival; the most favored passengers were women and children with firstor second-class tickets. In each of these examples, he creates visual displays of data to uncover patterns that are specific to these cases. Because there is no effort to generalize beyond the case at hand, calculations of statistical error are not relevant.

Yet another of Spiegelhalter's cases involves an English hospital's elevated death rates for heart surgery on children. Here the question is whether these bad results are attributable to insufficient experience with this type of surgery at the hospital in question. In this case he would like to general-


[^0]:    Brian Hayes is a former editor of and columnist for American Scientist. His most recent book is Foolproof, and Other Mathematical Meditations (The MIT Press, 2017).

